MATHEMATICS FLORIDA STANDARDS

Algebra 1

Program Overview and Sampler

AN AMSCO $^{\circ}$ PUBLICATION



Preparing for College and Career

The *Mathematics Florida Standards* program provides the foundation for Algebra 1 success. Students learn through direct instruction, discovery-based learning, and guided practice, allowing them to transfer skills to real-world situations, problem-solving activities, and the Florida Standards Assessment (FSA) End-of-Course (EOC). Through active discourse and collaborative activities, students learn to communicate effectively and gain the perseverance necessary to solve difficult problems.

Algebra

Learning Through Multiple Approaches

Discovery-Based Learning	Application
 Guided Instruction Guided Practice Connect to Testing 	 Concepts in the Real World Extension and Interactive Activities Authentic FSA EOC Practice
Personalized Practice	Direct Instruction
 <i>i-Practice</i> Personalized Assignments (Digital) Video Model Problems (QR Codes, Digital) Multiple Problem Help Options (Digital) 	 Lesson Introduction Words to Know Remediation Activities



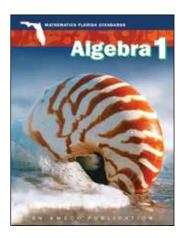
Student-Centered Approach to Algebra 1

The *Mathematics Florida Standards* program focuses on active learning. Engage students as they explore concepts, learn through guided instruction, and apply their knowledge in the extension and assessment activities.

Prepare Students for Success

Designed specifically for the Florida Mathematics Standards, the curriculum ensures that students will have the knowledge and skills that matter for both the FSA EOC and their college and career paths.

Program Components



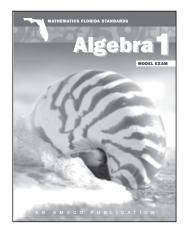
Student Worktext



Florida Algebra 1 Digital



Teacher Wraparound Edition



Model Exam

PERSONALIZED LEARNING

- Lesson videos, accessed through QR codes, provide students with model problems on demand.
- Digital assignments can be customized and delivered individually, to small groups, or to the whole class.
- Through *i-Practice*, each student can practice skills to mastery.



ACTIVE DISCOURSE AND MATH LITERACY

Throughout each lesson, students and teachers engage in whole class, small group, and peer discussions. Students develop communication skills and math literacy as they work with others to understand concepts, build skills, and tackle more complex problems.



DEPTH OF KNOWLEDGE (DOK)

Concepts, questions, and activities are carefully designed to meet the full range of Webb's task complexity. All practice and assessment items are tagged with DOK levels. Independent practice and chapter tests prepare students for the rigor of the Florida Standards Assessment End-of-Course as well as other complex tasks and projects.

4. Which of the following equations is not equivalent to the rest?

A. $y = \frac{1}{3}x - 7$ B. $y + 5 = \frac{1}{3}(x - 6)$ C. x - 3y = 21D. 3x - y = 21

(DOK 3)

ASSESSMENT

Each chapter and lesson focuses on specific learning outcomes with aligned formative and summative assessments. Items mirror those on high-stakes assessments with an emphasis on the Florida standards.

- Connect to Testing
- independent practice
- chapter-level and comprehensive FSA EOC practice
- diagnostic tests
- digital assignments, quizzes, and tests
- teacher-built assignments and tests using an extensive item bank and online assignment builder

chapter tests

DIFFERENTIATION

Support for ELLs, ESEs, and advanced students helps all students succeed and be challenged.

- Point-of-use vocabulary and math literacy support, remediation suggestions, and videos ensure content is accessible.
- Extension activities and a rich problem item bank ensure students remain challenged.

ELL

Provide the following sentence frames to help students respond to the RECAP question.

Beginning/Intermediate:

- One way to find slope is _____.
- This way is best for _____.
- Another way to find slope is _____.
- This way is best for _____.

Intermediate/Advanced:

- One way to find slope is _____.
- This way is most appropriate for
- Another way to find slope is _____
- This way is most appropriate for

DIGITAL ASSIGNMENTS, QUIZZES, AND TESTS

- *i-Practice* personalized assignments
- point-of-use support (videos, hints, step-bystep help) and smart feedback
- pre-built diagnostic, chapter, and summative tests
- FSA EOC practice
- technology-enhanced items (equation editor, multi-select, drag and drop, matching, and much more)
- multiple attempts allowed for homework and *i-Practice*
- print capability for offline assignments

Assignment i-Practice		Remaining 5	Mastered 0	Needs Worl
Question No: 1		Su	bmit Assign	ment >
Solve. 7a - 10 = 5a + 6 a =	00	Solving equations vector $4\chi = 15$ $\frac{4}{5} \times = \frac{15}{5}$ $\frac{5}{5} \times = \frac{15}{5}$ $\chi = 3$	side	e on
7a - 5 Combine like terms $7a - 3$	= 5a + 6 a - 10 = 5a - 5 5a - 10 = 0 + 6	•a + 6		
Remove the constant 2a -	-a - 10 = 6 - 10+ 10 = 6 + 10			
Add 2a+0 =			(<u>२</u> २

CLASS AND STUDENT ANALYTICS

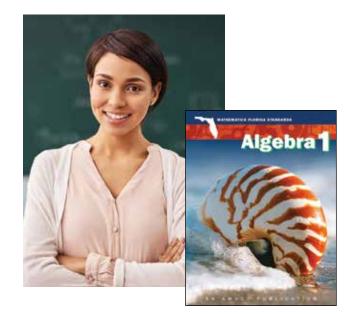
- performance measures by skill and Florida Mathematics Standard
- extensive drill down capabilities (class, student, item)
- visual highlighting of strengths and performance gaps

Terena Morris		Class: Agebra 1 •	Standard: ALL Standards	 Student; 	All Balances		
Assignments	>				All Dudents Allen, Violet Brown, Ava		
Standards	*	Standard *	Performance		Clark; Skylar	Problems	Average
Overvlew		Standard **	Performance		Cooper, Christopher Evans, Lucal		
Statent Reports		A-APR 1	7 15		Gonzalez, Allieon Harris, Samantha	5	69%
Standard Reports		A-APR 3	18		Jackson, Penelope King, Mason	1	82%
		A-APR 4	34		Lopez Audrey Miller Mia	2	82%
Problem List		A-CED 4	10 2 10		Morgan, Andrew Nelson, Alexander	12	75%
		A-SSE 2	1)		Perez Ariana Ramirez, Benjamin Robinson, Anna	7	83%
		A-SSE 3			tanches, troah Stewart, Gabriel	1	100%
		Func o Average 77%	6 14 4		Thompson, Riley	3	75%
		Excelling 10 students Passing E students	et, 19			1	0%
		Failing Estudents				6	6615

LESSON PLANNING AND INSTRUCTIONAL SUPPORT

The teacher wraparound edition, available in both print and digital formats, provides planning guidance for each chapter and lesson, including

- Chapter Planner
- chapter goals with sample problems
- lesson prerequisites and suggested pacing
- discussion questions and suggested answers
- guided practice objectives with implementation ideas to encourage active discourse



OPEN EDUCATIONAL RESOURCES

No more searching the internet for lessons and videos! Open educational resources are provided at point of use.

- reviewed and vetted by math educators to ensure usefulness and appropriateness
- videos, interactive activities, and lesson-specific activities using programs such as **Desmos** and **GeoGebra**
- one-click access to all suggested resources via the digital teacher edition

DIGITAL COURSE MANAGEMENT

Teachers can easily create, modify, and share digital assignments, quizzes, and tests. In addition, teachers can

- automate grading with instant feedback
- customize assignments
- create individual, group, and whole class assignments
- review answers and modify grades
- modify assignments and due dates

CHAPTER INTRODUCTION

Chapter Planner

includes standards, lesson prerequisites, sequencing, and representative sample problems. Lesson pacing suggestions are also available.

- Chapter Overview and Chapter Goals clearly state the learning objectives.
- Concepts in the Real World provides students insight into how chapter concepts are applied outside the classroom.

• Connect to Testing engages students in chapter concepts using a FSA EOCstyle example problem. Guided instruction and active discourse promotes student discovery of new concepts and their application.

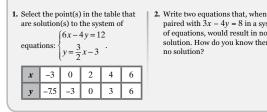
• Words to Know introduces chapter concept vocabulary.

Chapter Planner

The lessons in this chapter focus on writing, graphing, and solving systems of linear equations and systems of linear inequalities.

Lesson Alignment	When Do I Teach This Lesson?
Lesson 1 Graphing Linear Systems of Equations (MAFS.912.A-CED.1.2, MAFS.912.A-REI.3.6)	Students should know how to rewrite linear equations into slope- intercept form and how to graph linear equations.
Lesson 2 Solving Linear Systems by Elimination or Substitution (MAFS.912.A-REI.3.6)	This lesson could be split into two parts (substitution, elimination) if your students benefit from having more time to practice new skills.
Lesson 3 Creating Systems of Linear Equations (MAFS.912.A-CED.1.2, MAFS.912.A-REI.3.5, MAFS.912.A-REI.3.6)	Teach this lesson after demonstrating all methods of solving systems of linear equations.
Lesson 4 Systems of Linear Inequalities in the <i>xy</i> -Plane (MAFS.912.A-REI.12 MAFS.912.A-CED.1.3)	Prior to this lesson, discuss how to determine if an ordered pair is a solution to a linear inequality and how to graph linear inequalities including those with vertical and horizontal boundaries.

Chapter Sample Problems



Write two equations that, when
paired with 3x - 4y = 8 in a system
of equations, would result in no
solution. How do you know there is
no solution?3. Edita and Janina are buying school
supplies. Edita buys 5 notebooks
and 6 binders for a total of \$25,45.
Janina buys 4 notebooks and 8
binders for \$30,60. Boipelo later
goes to the same store and buys
3 notebooks and 2 binders. What is

his total?

Systems of Lin Inequalities in 1

Introduction

Chapter 4 Systems

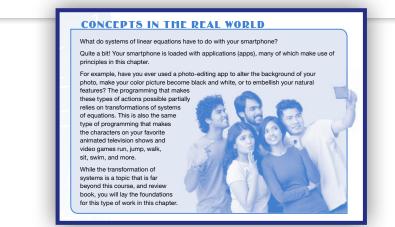
Chapter Goals:

Algebra 1

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- At the end of this chapter, students will be able to
- · graphically solve a system of two linear equations.
- algebraically solve a system of two linear equations using elimination or substitution.
- write a system of linear equations to model a given situation.
- represent constraints using inequalities.
- graph systems of linear equations in the *xy*-plane and shade the solution region.

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CONNECT TO TESTING

(DOK 3)

Directions: Read the question and work through the solution steps with a partner.

The system $\begin{cases} Ax + By = C\\ Dx + Ey = F \end{cases}$ has the solution (-4, 5), where A - F are all nonzero real numbers.

Select all the systems that are also guaranteed to have the solution (-4, 5).

A. $\begin{cases} (A+D)x+(B+E)y=C+F\\ Dx+Ey=F \end{cases}$ C. $\begin{cases} 3Ax+3By=3C\\ 2Dx+2Ey=2F \end{cases}$ B. $\begin{cases} (A+B)x+(D+E)y=C+F\\ Dx+Ey=F \end{cases}$ D. $\begin{cases} Ax+By=C\\ (D-4A)x+(B-4E)y=F-4C \end{cases}$

Understand It: You can solve systems of equations by graphing, substitution, or elimination. You can also use these methods for comparing systems.

Visualize It: Picture the given system mentally. Rearranging the equations in the given system into slope-intercept form, you see that they both have negative slopes and positive *y*-intercepts.

Solve It: Use the table below to organize your work.

Look carefully at the form of answer choice A. Try elimination and see if you can get the result into the form $(A+D)x+(B+E)y=C+F$. If so, answer choice A is correct.	Ax + By = CAnswer choice A is correct. +Dx + Ey = F $Ax + Dx + By + Ey = C + F$ $x(A + D) + y(B + E) = C + F$
Apply the same strategy to answer choice B, as it is of the same type as answer choice A. Use the space to the right for your work.	This answer is incorrect. While you can solve a system by adding one equation to another to rewrite it, you must group like terms together. In this case $Ax + By = C$ has been added to $Dx + Ey = F$, but like terms are combined incorrectly in the first equation.
Examining answer choice C reveals that it is the given system, except the first equation is multiplied through by 3 and the second equation is multiplied through by 2. Use the space to the right to show that answer choice C is correct.	Student work will vary. The simplest way to show this answer choice is correct is to divide the first equation by 3 and the second equation by 2.
For choice D, employ and combine the previous strategies to determine if it is a correct choice. Use the space to the right as needed.	Answer D is incorrect. You can solve a system by subtracting a multiple of one equation from another, you must be careful to group like terms together and to subtract in the same order. In this case, 4 times Ax + By = C is being subtracted from $Dx + Ey = F$ but (B - 4E)y is incorrect, it should be $(E - 4B)y$.

	WORDS TO KNOW	- a-			
	coinciding lines constraints	elimination parallel lines	substitution system of equations	system of linear inequalities	
¢	Perfection Learning® No reproduction perm	itted.		Chapter 4 Systems	95

CONNECT TO TESTING

Use these questions to help your students engage with the process of solving a simulated state test question.

 Before attempting the walk-through in the Solve It section, students should have a firm grasp of solving systems by elimination. Use the following problem as a remediation for students who need extra practice.

$$2x + 3y = 20$$

2x + y = 4

The solution is (-2, 8).

2. Ask students to make a plan to compare the systems in the answer choices to the system in the question. Prompt them to take the structure of the systems into account, if needed.

Student plans will vary. One strategy to solve this problem is to rewrite all the systems so they are in the same form. For the given system, slope-intercept form is

$$\begin{cases} y = -\frac{Ax}{B} + \frac{C}{B} \\ y = -\frac{Dx}{E} + \frac{F}{E} \end{cases}$$

From this students can see that both equations have negative slopes with positive *y*-intercepts.

LESSON: INTRODUCTION

- Each lesson begins with short, direct instruction and transitions to guided instruction.
- Discussion questions and interactive activities prompt active discourse and student discovery.
- Extension activities promote visualization and application of concepts.
- ELL activities such as sentence frames, vocabulary notebooks, and graphic organizers help build math literacy.
- Videos give learners additional support.

INTRODUCTION

How do you determine when to use substitution and when to use elimination to solve a system of equations?

Student answers will vary. One possible answer: Examine how the system is presented. If both equations are in slopeintercept form and don't have any fractions or decimals, I would use the substitution method. I would also use this method if one of the equations was solved for x or y. If both equations were in standard form, I would use the elimination method.

How does solving by elimination compare with solving by the substitution method?

The elimination method is used when both equations are in standard form. In this method you eliminate either the x or the y variable by first adding the equations. In the substitution method, you substitute one equation into the other in order to solve for one of the variables.

Why is it sometimes important to use the elimination or substitution method rather than the graphing method to solve a system of equations?

It is not always easy to graph systems of equations accurately by hand. Additionally, if the solution is fractional, it can be difficult to read from the graph.

LESSON 2

Solving Linear Systems by Elimination or Substitution

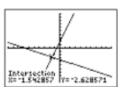
INTRODUCTION Elimination and Substitution

Sometimes it is hard to find the solution to a system by graphing. Consider

y = 3x + 2the system

 $y = -\frac{1}{2}x - 3\frac{2}{5}$

These lines intersect and the system has a single solution, as shown at the right. However, the coordinates of the intersection point, (-1.54, -2.63), are not integers. You can find approximate values using the intersection feature on a graphing calculator, but you could not find an accurate solution if you graphed this system by hand. Luckily, there are two additional methods for solving systems of equations-elimination and substitution



Elimination	Substitution
Main Idea:	Main Idea:
 Add the two equations together so that one variable is eliminated. 	• Substitute an expression for one variable into the other equation.
When to Use:	When to Use:
• Often easiest to use when the equations are in standard form, $Ax + By = C$.	• Often easiest to use when one or both equations has one variable isolated or is in <i>y</i> = <i>mx</i> + <i>b</i> form.

Consider the example where a system is solved using elimination

$\begin{array}{c} 2x + 5y = 7 \\ 3x + 5y = 13 \end{array}$	
5x + 0y = 20	
5x = 20 $x = 4$	
2x - 5y = 7 2(4) - 5y = 7 8 - 5y = 7 -5y = -1 $y = \frac{1}{5}$	3x + 5y = 13 3(4) + 5y = 13 12 + 5y = 13 5y = 1 $y = \frac{1}{5}$
	5x = 20 x = 4 $2x - 5y = 72(4) - 5y = 78 - 5y = 7-5y = -1$

EXTENSION ACTIVITIES

Activity

Solving Linear Systems Algebraically

In this activity, students will solve linear systems algebraically and then drag the solution point to the intersection, if any, of the graph. (Approximately 20 minutes)

https://www.geogebra.org/m/NHYqDPnS

LESSON: GUIDED INSTRUCTION

			$\left(\begin{array}{c} - \end{array} \right)$
Solving Linear Syste	ms by Eliminatio	on or Substitution	LESSON 2
Now, consider an example using <u>substitution</u> .			
(²	211 211 4	2 6 4	

Solve the system $\begin{cases} y = \frac{2}{3}x \\ 2x + 3y = 4 \end{cases}$ Substitute the expression $\frac{2}{3}x$ for <i>y</i> in the second equation. Then simplify and solve the equation for <i>x</i> .		· ·
Now substitute the value found for <i>x</i> into one of the original equations to find <i>y</i> .	$y = \frac{2}{3}(1)$ $y = \frac{2}{3}$	2(1) + 3y = 4 2(1) + 3y = 4 2 + 3y = 4 3y = 2
The solution is the coordinate point $\left(1,\frac{2}{3}\right)$		$y = \frac{2}{3}$

GUIDED INSTRUCTION Other System Solutions

When solving a system using elimination or substitution, <u>all</u> the variables will disappear when there is no solution or infinitely many solutions.

Ostation	A Question with the first state Manuel Quelotion of
Solution	A System with Infinitely Many Solutions
$\int y = 2x - 1$	4x + y = 7
$\begin{cases} y = 2x - 1\\ -2x + y = -5 \end{cases}$	$\begin{cases} 4x + y = 7\\ 8x + 2y = 14 \end{cases}$
• Substitute $2x - 1$ in for <i>y</i> in the second equation. Then simplify and solve.	• No variables are eliminated when the equations are added together, so you need to multiply the first equation by -2.
-2x + (2x - 1) = -5 -2x + 2x - 1 = -5	$-2(4x + y) = -2(7) \rightarrow -8x - 2y = -14$
0 - 1 = -5 -1 = -5	Add this to the second equation. Then simplify and solve.
	-8x - 2y = -14
The variables are gone and you are left with the	$\frac{+8x+2y=14}{0x+0y=0}$
statement $-1 = -5$, which is <u>false</u> .	0 = 0 The variables are gone and you are left with the
When the variables cancel and the statement is	statement $0 = 0$, which is <u>true</u> .
false, there is no solution.	When the variables disappear and the statement is true, there are infinitely many solutions.
	statement $0 = 0$, which is <u>true</u> . When the variables disappear and the stateme

RECAP

1. Describe a situation in which each solving method would be preferable.

Student answers will vary. Generally, graphing would be a useful method if the solution is a point with small integer coordinates and whose equations are easy to graph in slope-intercept form. Elimination is a useful method if the equations are both in standard form so the x, y and constant terms are in the same order in each equation. Substitution is a useful method when one of the equations has one of the variables already isolated, or if both equations are in slope intercept form.

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Lesson 2 Solving Linear Systems by Elimination or Substitution 103

Video

Solving Systems of Equations Using Elimination By Addition

Explains how to solve systems of linear equations using the elimination method. (Length: 9:59)

https://www.youtube.com/watch?v=ej25myhYcSg

Instruction

ELL VOCABULARY

• Ask students to record the following academic vocabulary and definitions in their Vocabulary Notebook: *additional** (another), *stacked* (placed on top of each other), *either* (one or another), *neither* (not one or the other), *description* (a statement/ sentence that tells what something is like), *paired* (joined in groups of two), *individually* (one at a time, alone), *exact* (fully or completely accurate, correct).

_		
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_	_	<u> _ (</u>
		N

Provide the following sentence frames to help students respond to the RECAP question.

Beginning/Intermediate:

- *Graphing is better when* _____.
- Elimination is better when _____
- Substitution is better when _____

LESSON: GUIDED PRACTICE

- Each activity has a clearly stated purpose and stepped-out support.
- Scaffolded practice provides opportunities for small group and peer-to-peer discussions.
- Remediation activities provide reteaching and reinforcement opportunities.
- All guided practice activities include DOK levels.

GUIDED PRACTICE

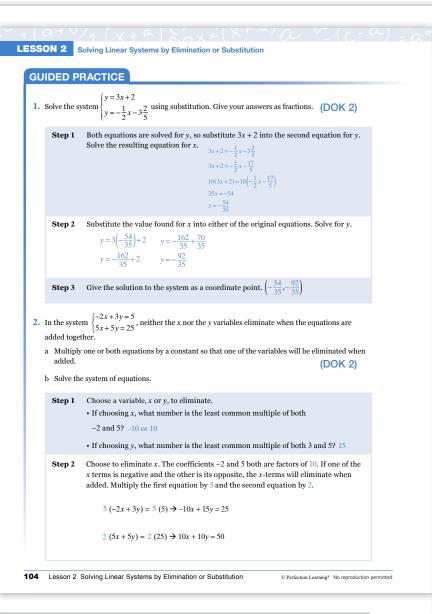
Question 2 Remediation: Table Activity

Purpose

This activity gives students more practice with solving by elimination.

Implementation

- Copy the table below, without answers, onto the board, or display using projection equipment with the answers covered.
- Have the students complete the chart individually or in pairs, placing a check mark in the column "Elimination" or "Substitution" to show which method would be best for solving the given system.
- Students can solve the systems or you can lead the class in solving each of them, discussing why certain methods are preferable.



System	Elimination	Substitution	Solution
$\begin{cases} 2x + 3y = 12\\ 2x - 3y = -6 \end{cases}$	1		$\left(\frac{3}{2},3\right)$
$\begin{cases} 6x - 2y = 14\\ y = -\frac{1}{2}x \end{cases}$		4	(2,-1)
$\begin{cases} 5x + 3y = 14\\ 3x - 3y = 18 \end{cases}$	4		(4,-2)
$\begin{cases} 4x - 3y = 19\\ 5x + 3y = 17 \end{cases}$	4		(4,-1)

		olving Linear Systems by El		- (L.) _ ISON 2	
Step 3	Add the equations a -10x+15y=25 +10x+10y=50 25y=75 y=3	nd solve for the variable in th	e space below.		• For Guided Practice #3, use images or sketches to explain the words: <i>hamburgers, fries</i> .
Step 4	Substitute the varial variable. -2x + 3(3) = 5 -2x + 9 = 5 -2x = -4 x = 2	ble value into either original e	quation to solve for the other		
Step 5	Write the solution a	s a coordinate point. (2,3)			
y = 2 repre	sents Number of Ham sents Number of Fries of Hamburgers of Fries Consider what each you solving for in co below.	Cost of Hamburgers Cost of Fries variable means in the system.	(DOK 1) Total Items Total Cost When you solve for <i>x</i> , what are bout <i>y</i> ? Answer these questions		
	x represents the num	incer of naniburgers and y repr	esents the number of fires.		
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LESSON: PRACTICE

- Practice activities cover a range of DOK levels.
- QR codes link to instructional videos supporting the assignment.
- Full solution explanations are provided at point of use.

2. Use the substitution method. Solution steps are shown. 2(2y+8) - 3y = 184y + 16 - 3y = 18v = 2Then x = 2(2) + 8 = 12.

3. Eliminate answer choice A as the lines are parallel. Check answer choice B:

$$3x + 2\left(\frac{-3}{2}x + 4\right) = 8$$
$$8 = 8$$

A true statement results so this system has infinitely many solutions. Do the same for answer choice C:

$$-8\left(\frac{-1}{4}y + \frac{3}{4}\right) - 2y = -6$$

-6 = -6

Again, this system has infinitely many solutions.

For answer choice D,

$$4x - 6\left(\frac{2}{3}x - 3\right) = 9$$

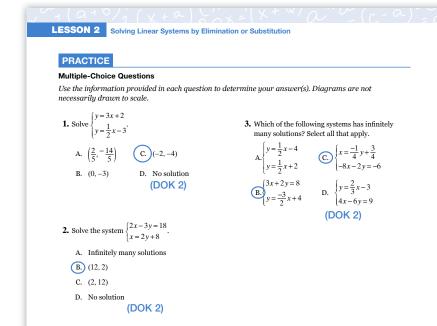
18≠9

This is a false statement, so this system has no solution and is not a correct choice.

- 4. Rewrite the equation 3x 4y = 8 in slope-intercept form: $y = \frac{3}{4}x + 2$. Any equation with the same slope but different y-intercept will have no solution when paired with it in a system.
- 5. Use the elimination method. Solution steps are shown.

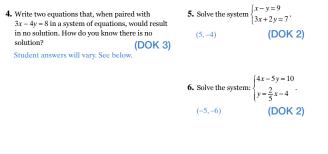
$$2[x - y = 9] \rightarrow 2x - 2y = 18$$

+3x + 2y = 7 \rightarrow +3x + 2y = 7
5x = 25
x = 5



Open-Response Questions

Use the information provided to answer the questions in this part. Clearly indicate all your steps, and include substitutions, diagrams, graphs, charts, etc., as needed. Diagrams are not necessarily drawn to scale.



106 Lesson 2 Solving Linear Systems by Elimination or Substitution

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Solve for y. 5 - y = 9v = -4

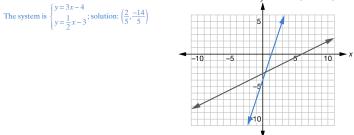
6. Use the substitution method. Solution steps are shown.

 $4x - 5\left(\frac{2}{5}x - 4\right) = 10$ 2x = -10x = -5Solve for *y*. 5

$$y = \frac{2}{5}(-5) - 5$$
$$y = -6$$

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i. $-6x - 15y = -1$		for each system? Match each equat a. No solution	(DOK 3)
ii. $3x - y = 16$	d.	b. Infinitely man	y solutions
iii. $y = -\frac{2}{5}x + 4$	a.	c. (0, 1)	
iv. $3x - 4y = -4$	с.	d. (5, -1)	



9. Kweku solved the system $\begin{cases} 2x + 4y = 9 \\ -3x - 6y = 2 \end{cases}$, but made a mistake. His work is shown below. At which step did he make a mistake? What is the actual answer?

Step 1: $\begin{cases} -3(2x+4y=9)\\ 2(-3x-6y=2) \end{cases}$	Step 4: $y = \frac{23}{24}$	The mistake is in Step 1. There is no solution to this system.
Step 2: $\begin{cases} 6x - 12y = -27 \\ -6x - 12y = 4 \end{cases}$	$2x + 4\left(\frac{23}{24}\right) = 9$ Step 5: $2x + \frac{23}{6} = 9$ $2x = \frac{31}{6}$	
Step 3: -24 <i>y</i> = -23	$2x = \frac{31}{6}$ $x = \frac{31}{12}$	

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Lesson 2 Solving Linear Systems by Elimination or Substitution 107

Substitute this value for *x* in either equation and solve for *y*:

$$y = 3\left(\frac{2}{5}\right) - 4 = \frac{-14}{5} \,.$$

9. If Kweku wanted to eliminate the *x*-variable, he should have multiplied the equations by +3 and +2, since the *x* terms already had opposite signs. If he had, the system would have become (6x + 12y = 27)

$$\begin{cases} -6x - 12y = 27 \\ -6x - 12y = 4 \end{cases}$$
. Summing these

equations eliminates both x and y, resulting in 0 = 31, which is not true. The system has no solution.

Review

7. Consider each potential system.

$\begin{cases} 2x + 5y = 5\\ -6x - 15y = -15 \end{cases}$	$\begin{cases} 2x + 5y = 5\\ 3x - y = 16 \end{cases}$
These equations are the same; the second is equivalent to the first equation multiplied through by a factor of –3.	Use elimination to solve. 2x+5y=5 15-5y=80 17x=85 x=5 There is only one answer choice with an <i>x</i> -value of 5.
Infinitely Many Solutions (b)	(5, -1) (d)
$\begin{cases} 2x+5y=5\\ y=-\frac{2}{5}x+4 \end{cases}$	$\begin{cases} 2x+5y=5\\ 3x-4y=-4 \end{cases}$
Use substitution to solve. $2x + 5\left(-\frac{2}{5}x + 4\right) = 5$ $2x - 2x + 20 = 5$ $20 \neq 5$ This is a false statement.	Use elimination to solve. Multiply the first equation by -2 and the second by 3. Then -6x + 8y = 8 6x + 15y = 15 23y = 23 y = 1 There is only one answer choice with a
No Solution (a)	<i>y</i> -value of 1. (0, 1) (c)

8. Write the system using the *y*-intercepts and a second point on each line. The system is

$$\begin{cases} y = 3x - 4\\ y = \frac{1}{2}x - 3 \end{cases}$$

Solve by substitution.

$$\frac{1}{2}x - 3 = 3x - 4$$
$$x = \frac{2}{5}$$

OPEN EDUCATIONAL RESOURCES

- Save time with carefully curated open resources.
- Open resources include interactive activities, simulations, videos, and digital tools.
- Time estimates and activity synopses are provided to assist in planning and usage.

INTRODUCTION

Give an example of a problem that could be solved using a system of linear equations.

Student answers will vary. Any situation that relates two variables using two linear equations is appropriate.

Explain how to write a system of equations from a word problem.

Student answers will vary. One possible answer: To write a system of equations from a word problem, I must first determine how many variables are in the problem. The number of unknown variables tells me how many equations I will need in order to solve my unknowns. Then I need to look at the context for clues, breaking down the problem sentence by sentence.

GUIDED INSTRUCTION

How can you determine if two given systems of equations are equivalent?

Student answers will vary. One possible answer: I can determine if two systems of equations are equivalent by transforming each equation into slope-intercept form. If they are equivalent, the equations will be the same for both systems.

LESSON 3 Creating Systems of Linear Equations

INTRODUCTION Writing Linear Systems

 A gym sells day passes for use of the pool and use of the racquetball courts. Passes for the pool cost \$3.50 per day and passes for the racquetball court cost \$4.00 per day. In one month, Alida spends \$53.50 on passes and goes to the gym 14 times. How many times did Alida go to the pool and to the racquetball court? Write and solve a system of equations.

Determine what is being asked. In this case, you are being asked, "How many times did Alida go to the pool and to the racquetball court?"	x = number of visits to the pool
• Define two variables for the two unknowns in the box to the right.	y = number of visits to the racquetball court
There is information about the cost and about the number of passes in the sentence, "In one month, Alida spends \$53.50 on passes and goes to the gym 14 times."	Write an equation regarding the cost of the passes: $3.5x + 4y = 53.50$
• Use <i>x</i> and <i>y</i> and the information in the sentence to write two equations.	Write an equation regarding the number of passes: $x + y = 14$
Solve the system.	Solve the equation $x + y = 14$ for <i>y</i> . y = 14 - x
The equation $x + y = 14$ can be easily solved for \hat{y} . Solve this equation to the right.	
Solve the system using substitution in the space below $3.5x + 4(14 - x) = 53.5$ $-0.5x = -2.5$ $x + y = 14$ $3.5x + 56 - 4x = 53.5$ $x = 5$ $5 + y = 14$ $-0.5x + 56 = 53.5$ $y = 9$	κ.
Answer the following questions in the box to the right. • How many times did Alida go to the pool? • How many times did Alida go to the racquetball	Pool visits: 5 Racquetball court visits: 9
court?	Kacquetban court visits: >

GUIDED INSTRUCTION Choosing the Correct System

Prasad is 5 years older than Jamal. Jamal is twice the age of Menuha. Together, the ages of Prasad, Jamal, and Menuha sum to 50. How old are Prasad, Jamal, and Menuha? Consider the systems of equations shown in the table at the top of the next page. To choose the correct system. check the following.

- Does the system have the correct number of variables?
- · Do the equations match the given information?

108 Lesson 3 Creating Systems of Linear Equations

· Solve the system. Does the answer make sense given the information in the problem?

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EXTENSION ACTIVITIES

Activities

Linear Systems: Gym Membership

This is an extension you can use after students are comfortable creating linear equations. (Approximately 40 minutes)

https://teacher.desmos.com/activitybuilder/ custom/561d6a790784861e06c3a6dc#

Systems of Linear Equations

Here students will write systems of equations from word problems and then graph the equations on the *xy*-plane. (Approximately 20 minutes)

https://www.geogebra.org/m/Vtd7Xaas

Creating Systems of Linear Equations

LESSON 3

Instruction

System 1 System 2 System 3 P+J+M=50 P+J+M=50 P=J+5 J=P+5 P=J+5 J=2M

The ages of Prasad, Jamal, and Menuha are unknown. In the systems above, how are the variables defined?

- P = Prasad's age
- J = Jamal's Age
- M = Menuha's Age

Consider the first sentence: "Prasad is 5 years older than Jamal." Which equation listed above best describes this relationship? P = I + 5

Consider the second sentence: "Jamal is twice the age of Menuha." Which equation listed above best describes this relationship? l = 2M

Consider the third sentence: "Together, the ages of Prasad, Jamal, and Menuha sum to 50." What equation can be written to show this sum? P + I + M = 50

Which is the correct system? System 2

Solve the correct system in the box below, checking your answer as shown.

P+J+M=50 $P=J+5$ $J=2M$	Solution continued
Substitute 2M for J in the second	Simplify and solve for M .
equation.	5M + 5 = 50 $5M = 45$ $M = 9$
P = 2M + 5	If $M = 9$, then $J = 2(9)$, $J = 18$.
Write the first equation in terms of M .	If $J = 18$, then $P = 18 + 5$, $P = 23$.
Let $P = 2M + 5$ and $J = 2M$.	Check:
P + J + M = 50 $(2M + 5) + 2M + M = 50$	Is Prasad 5 years older than Jamal? Yes Is Jamal twice the age of Menuha? Yes Is the sum of the ages 50? Yes

• If there are two unknown variables, there will be two equations in the system. If there are three unknown variables, there will be three equations.

RECAP

1. Generally, which part of a problem helps you to determine what the variables are? Use examples from the lesson to explain your answer.

Student answers will vary. Generally, the question at the end of a problem tells what is unknown, such as the ages of people, or the number of times visited to the pool or court.

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Lesson 3 Creating Systems of Linear Equations 109

Video

Systems of Linear Equations in Two Variables

Reiterates the importance of the intersection point. Walks students through a problem and solution. (Length: 6:37)

https://www.youtube.com/

watch?v=75m60SxFfJg&t=190s

- For the introduction problem, use images or sketches to explain the words: gym, pool, racquetball, passes.
- Ask students to record the following academic vocabulary and definitions in their Vocabulary Notebook: *real world* (in life, not just in the classroom), *make sense* (to be clear or correct), *justify** (give reasons for), *verbal* (with words), *corresponding** (matching, being the same as), *interpret** (to explain, to figure out), *exceed** (to be greater or more than, to go over), *state* (to say).
- Have students review the following math vocabulary from Chapter 4: Lesson 1: system of equations* Lesson 2: substitution*, elimination* Chapter 2: Lesson 1: coordinates* Chapter 1: Lesson 1: sum* Lesson 2: equation*, variable*, multiplying*, equivalent Lesson 4: solution*.

VISUALIZATION AND MODELING

- Modeling and visualization activities help students deepen understanding.
- Comparing models promotes discovery and stimulates active discourse.

GUIDED PRACTICE

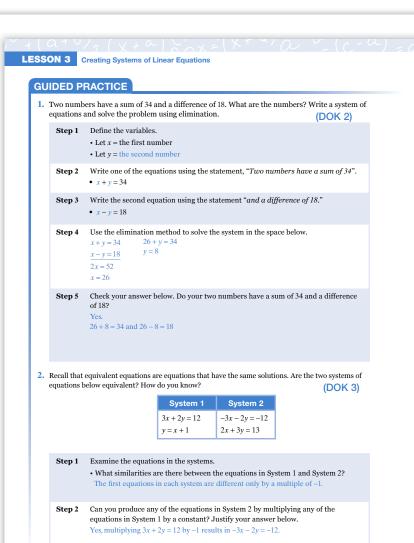
Question 1: Visual Summary

Purpose

In this activity, students create their own visual summary of a process to help them translate word problems into systems of equations.

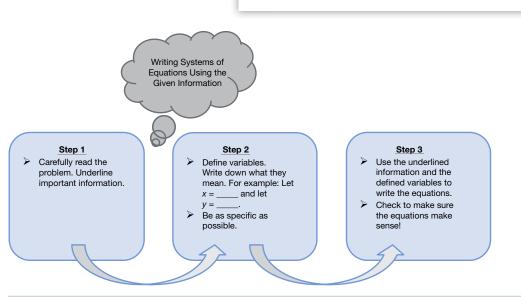
Implementation

- Divide students into pairs or have them complete this task individually.
- Consider providing a framework for the visual summary, or allow students to create their own. A sample is shown below.
- Once students have completed their visual summary, select a few to share, or complete a class visual summary to be displayed on the classroom wall for reference.



110 Lesson 3 Creating Systems of Linear Equations

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110 Algebra 1

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FLORIDA STANDARDS ASSESSMENT EOC PRACTICE

								• Each chapter concil EOC practice.	Jaes
CH/	APTER 4	FS	SA Pr	actice	×10		a) ⁻	 Each chapter test it a DOK level. 	em is
	rections: Carefully oice or by writing yo			nd then answer by some space provided.	electing the be	est available			
1.	. Organize the given systems of equations under their correct description by writing them in the table under the correct column. (DOK 2, Lesson 1) Systems of Equations:								
	A pair of parallel lines.	$\begin{cases} y+2=6\\ 0=-6x \end{cases}$		$\begin{cases} 3 = -3y - 3x \\ -y = x - 3 \end{cases}$					
	$\begin{cases} 3-x=-y \\ 1-z \end{cases}$	Two lines	s that at a point	Two lines that coincide.				FSA PRACTICE	
	$\int -y = -1 - 5x$ No Soluti		-	One Solution	Infinitely	Many Solutions		1. Solutions and explanations to the right.	are sho
	A pair of parallel lin (Parallel lines have common points.) $\begin{cases} 3 = -3y - 3x \\ -y = x - 3 \end{cases}$ (These lines have the	nes. no ne same	Two lines point. (Two line one point $\begin{cases} 3-x=-\\-y=-1 \end{cases}$ (These equations)	s that intersect at a es that intersect at only t have one solution.) -y	Two lines that (Coinciding I line and they common.) $\begin{cases} y+2=6x\\ 0=-6x+2+y \end{cases}$ (Rewrite bot	at coincide. lines are the same have all points in the equations in the torm. They are		2. (PART A) Write two equations express the relationship and variables. One equation shows the molds per minute to the number of chocolates needed minute and the other equations are equated with the model.	ong the uld rela total ed per
2.	hearts and one that r minute and the coin purchase 10 molds a purchase? PART A Let x re coin mo	makes choce mold can m nd produce present the olds. Fill in y's questio y = 460 0	olate coins. 1ake 40 cho 460 choco e number of the blanks n.	pes of chocolate mold The heart mold can r colate coins per minut lates per minute. How of heart molds and y is to write a system of em from PART A.	nake 60 chocola te. The compar many of each t represent the equations tha	ate hearts per ny wants to type should they number of		relate the total number of m company wants to buy to th The variables are defined in of the problem so the two ex- are $60x + 40y = 460$ and x (PART B) Solve using any of methods. Using substitution 60x + 40(10 - x) = 460 60x + 400 - 40x = 460 20x + 400 = 460 20x = 60 x = 3 y = 10 - 3 = 7	holds the varia the text quation y = 1 of the
	7 coin r							The company should buy 3 molds and 7 coin molds.	heart
120	Chapter 4 Systems -	— FSA Pract	lice	A. 2 <i>y</i>	$=\frac{2}{3}x+8$	C. $y = -\frac{1}{3}x +$	4	FSA Practice CHAPTER ate a system with no solutions? (DOK 3, Lesson 2)	/ <i>e</i> () 4
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- Each chapter concludes with FSA
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FSA Practice	CHAPTER 4
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FLORIDA ALGEBRA 1 DIGITAL

Student Application

Driven by the powerful *Math^x* personalized practice and assessment system, the student application provides a full range of assignments and practice aligned with *Mathematics Florida Standards Algebra 1,* including

- i-Practice personalized assignments
- online homework assignments
- quizzes and chapter tests

- diagnostic tests
- Florida Standards Assessment EOC practice

i-PRACTICE PERSONALIZED PRACTICE

Each *i-Practice* assignment can be customized to small groups or individual students. By focusing on specific skill areas, students can practice their way to success.

- Incorrect answers automatically generate new problems for students to attempt.
- A scoring counter shows progress on the assignment.
- Guided practice provides point-of-use help.
- Students have the option to stop and return to the assignment at any time.

Question No: 5		5.6	references >
Solve the inequality: 8x-15<21+7x	@ @ @	Brind Doltars, Sur Generation Benachter	ourate
	Remaining	Mastered	Needs Work
	2	2	

GUIDED PRACTICE ASSISTANCE

For *i-Practice* and homework assignments, students have a wealth of help accessible next to the problem. By providing multiple help options, the program addresses different learning styles and ability levels.

- Video provides step-by-step instruction for a similar problem.
- Step-by-Step Help guides students through each step of a multi-step problem.
- A help button gives problem hints and tips.
- Smart feedback responds to students' incorrect answers with suggestions.

Step by Step Help	
Collect like terms	7a - 8 = 4a + 7 $7a - 4$ $\cdot a - 8 = 4a - 4$
Combine like terms	7a - 4a - 8 = 0 + 7 $3 - 8 = 7$
Remove the consta	nt $3a - 8 + $ = 7 + nt on the left, which is -8, to get the <i>a</i> term by itself.
Add 8 to both sides	

ONLINE HOMEWORK, QUIZZES, AND TESTS

Assignments allow students the flexibility to answer questions in any order and give immediate feedback once an answer is submitted.

- Homework parameters set by the teacher allow multiple tries.
- Help functions (videos, hints/tips, step-by-step) appear for homework.
- Quizzes and tests eliminate the help functions automatically. Tests allow only one try. Quizzes allow for one or more tries, as set by the teacher.
- Assignment due dates, grades, and teacher communications are all easily visible from the student dashboard.

4	pher 1	Score: 10/40
0	Allow a to be a referral number and y to be an instituted number. Which of the following statements is board	0/5
2	which of the following is equivalent to $2(r-2)+1\sim 3(2r+1)^2$	5/S
3	Solve $\frac{d-2}{2} + 4 - s - 4$.	5/5
	Which number line (represents the solution to the inequality $3(3-2\alpha<457)$	0/5
9	By definition, a number set is closed under a given operation if you can show performing that operation within the set always produces another members of the set. Is the set of institunal numbers closed under the operation of multiplication? If so, verify in the space below. If not, provide a counterexample to well's your response.	0/5

TECHNOLOGY-ENHANCED ITEMS

Research shows that content mastery requires the ability to respond to a wide range of problem formats. Problem types include

- multi-part problems
- equation input
- graphing
- drag and drop
- multi-select
- open response
- and much more ...

Which of the following equations represents y, the hole cubes? y = 2x + 25 $y = \frac{1}{2}x + 25$ y = 25x + 2 $y = \frac{1}{2}x + 2$	ght of the water in the jar after adding a ice
Part B If the beight of the water increases by Einches, how know? Down (B) (C) (B) (C) (C) (C) (C) (C) (C) (C) (C) (C) (C	Slope of Zero: Undefined Slope: Positive Slope: Negative Slope: (3.0).(-11,-15) (5,-3 (3.0).(-11,-15) (5,-3) (5,-3 (3.0).(-11,-15) (5,-3)

ent at her house. She dropped ice into a jar of water and then recorded

FLORIDA ALGEBRA 1 DIGITAL

Teacher Application

Driven by the powerful *Math^x* personalized practice and assessment system, the teacher application provides a full range of assignment, reporting, and grading functions. Comprehensive alignment with *Mathematics Florida Standards Algebra 1* provides teachers the ability to monitor student progress in real time and customize assignments based on performance.

PRE-BUILT ASSIGNMENTS

Each assignment is aligned with the *Mathematics Florida Standards: Algebra 1* lessons. Pre-built assignments include

- *i-Practice*, homework, quizzes, chapter tests, FSA EOC model exams, and diagnostic tests
- one-click due date assignment
- standards covered by each lesson with rollover explanations for the standards
- easy assignment modification functionality



CUSTOMIZABLE ASSIGNMENTS AND TESTS

Modify the pre-built assignments or create your own.

- Choose from thousands of items by standard or by lesson.
- Differentiate assignments for small groups or individuals.
- Create unique assignments for each student using "vary the parameter" technology.
- Print assignments for pencil and paper exercises.

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REAL-TIME PROGRESS MONITORING

Grade book functions allow teachers to monitor student progress in real time.

- assignments are automatically graded at time of submission
- at-a-glance look at student and class performance across homework, quizzes, and tests
- one-click access to individual student performance
- manage due dates and late assignments for individual students
- add/drop grades
- export function for district grade books

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EXTENSIVE REPORTING CAPABILITY

Reporting and drill-down functions allow teachers to

- assess class and student performance by standard or lesson
- identify students and topics for reteaching and remediation
- group students by ability and performance levels
- evaluate item-level performance by class and by student

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The **Mathematics Florida Standards** program provides the foundation for Algebra 1 success. Designed specifically for Florida, each standardsbased lesson helps students identify areas of weakness, receive targeted instructional support and practice, and prepare for the Florida Standards Assessment End-of-Course.

Students engage in active discourse to build math literacy through

- discovery-based learning
- direct instruction
- personalized practice
- real-world application, extension activities, and authentic FSA practice

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For more information on the Mathematics Florida Standards program, visit perfectionlearning.com/fl-algebra-1